Fork and D/y/d Connected Transformer Supplied 12-Pulse Uncontrolled Converter fed Retrofit Vector Controlled Induction Motor Drive: A Comparative Study

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***Abstract*— This paper presents a comparative investigation when a 12-pulse, uncontrolled converter fed retrofit Vector Controlled Induction Motor Drive (VCIMD) is supplied from D/y/d and Fork transformers, respectively. The study proves that Fork configuration results into reduction of total transformer magnetic rating when compared to D/y/d configuration, at almost same power quality performance level, observed on Full Load (FL) and Light Load (LL), respectively. VCIMD performance is compared under starting and load perturbation modes suitable for various industrial applications. The investigation is realised in MATLAB environment using Simulink and Sim Power System (SPS) toolboxes in Discrete Time Frame (DTF).**

***Keywords— D/y/d, Fork, Retrofit, Vector Controlled Induction Motor Drive (VCIMD).*** I. INTRODUCTION

Three- phase, squirrel-cage induction motors have been widely used for fixed-speed applications due to their simplicity, compactness, ruggedness, reliability, high efficiency, low cost and lesser maintenance .Vector Control technique introduces adjustable frequency operation for variable speed applications. Motor dynamics observed are similar to that of separately excited dc motor. The control technique uses two decoupled control signals, one responsible for control of excitation and other for control of torque respectively [1-5].

A block schematic of Indirect VCIMD is shown in Fig.1. The system consists of a three-phase, Voltage Source Inverter (VSI), a three-phase, squirrel cage induction motor and necessary control . Speed error ω re is processed to generate reference torque command T \*. A suitable value of excitation reference *i mr* \*is generated depending on the rotor speed. The VSI is operated in Current Control (CC) mode.

Non-Linear loads such as power electronic converters, draw non-sinusoidal currents from the supply and affect other users [6-12]. Techniques based on pulse multiplication, realised through suitable transformer connections, are discussed in [13-16] for power quality improvement of retrofit loads.

This paper targets towards a comparative investigation between Fork and D/y/d transformer connections and also proves that for the same VCIMD , fork results into lower

rating magnetics than that of D/y/d with similar performance level.

Sections II and III explain design of D/y/d and Fork transformers, respectively for retrofit VCIMD. Drive dynamics and supply end power quality details are presented in Section-IV. The detailed mathematical formulation for calculating magnetic ratings of Inter-Phase Reactor (IPR) and power transformer are also presented in this section. The result proves that for the same drive rating, total magnetic rating of Fork is lesser as compared to D/y/d .

II. DELTA/STAR/DELTA CONNECTED TRANSFORMER SUPPLING

12-PULSE, AC-DC, UNCONTROLLED CONVERTER FED RETROFIT VCIMD

*A. Rating Computation for D/y/d Transformer:*

Fig.2 shows the block schematic of D/y/d connected transformer, supplying 12-pulse, uncontrolled converter fed VCIMD. As the transformer has isolation, inter- converter currents are not possible. IPR connected between dc positive terminals of the converters neutralise instantaneous voltage difference between the two converters at the output port.

For a six-pulse, uncontrolled converter, the DC-Link output voltage, *V d*expressed as a function of transformer secondary line voltage, *VL* is,

V d = 3 π 2 V L (1) For design simplicity, it is assumed that the load current drawn from DC link ( i d) is constant in nature ( I d) due to highly inductive nature of the load. Fig.3 shows respective current waveforms at secondary and primary sides of the transformer and the resultant line current drawn from utility. Currents i 1', i '2, i 3'and i 1'', i ''2, i 3''are respective input currents to the 12-pulse, uncontrolled converter. Phase currents of the secondary delta winding, i I, i II and i III can be obtained as, i I = i 1 '' − i '' 2 3,

i II = i '' 2 − i '' 3 3and

i III = i '' 3 − i 1 '' 3(2) Phase current at the primary side, i atherefore computes to

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'i a = i 1

3 + i I (3) Similarly, i band i cget computed. The RMS phase currents at secondary star ( I phs ), secondary delta ( I phd ) and primary delta ( I php ), from Fig.3, are computed as, I phs = 0.4082I d , I phd = 0.2357I d and I php = 0.4552I d (4) Hence, rating of secondary star winding ( VA SS ) can be obtained as, VA SS = 3 × V phs × I phs = 0.5235P d (5) where, *P d*refers to power drawn from the DC link. Similarly, rating of secondary Delta ( *VA SD* ) and primary Star ( *VA P* ) get computed as, VA SD = 3 × V phd × I phd = 0.5235 *P d*(6) VA P = 3 × V php × I php =1.0112 *P d*(7) Therefore, total rating of D/y/d transformer amounts to,

Fig.2. Block Schematic of D/y/d Transformer Supplying 12-Pulse,

Uncontrolled Converter fed Retrofit VCIMD

VA D/y/d = VA Pr imary + 2VA Sec ondary

= 1.0291P d

(8)

*B. Design of Inter-Phase Reactor (IPR)*

Line voltages on star secondary can be stated as, V a ' b ' = 2V L Sin( ω t + 30 ° ) (9)

Fig.1. Block Schematic of Vector Controlled Induction Motor Drive

' ' L b c V 2V Sin( t 90 ) = ω − ° (10)

' ' L c a V 2V Sin( t 150 ) = ω + ° (11)

Similarly, secondary delta voltages,

'' '' L a b V 2V Sin t = ω (12) '' '' L b c V 2V Sin( t 120 ) = ω − ° (13)

'' '' L c a V 2V Sin( t 120 ) = ω + ° (14) Voltages across IPR can be expressed as pq po qo v v v = − (15) po v and qo v shown in Fig.2, can be obtained for various

Fig.3. Current Waveforms for D/y/d transformer supplying 12-

Pulse Uncontrolled Converter fed Retrofit Constant Current Load:{a}=0.5Id;{b}=0.0576Id;{c}=0.1153Id; {d}=0.0341Id; {e}=0.5576Id; {f}=0.9659Id; {g} =1.1153Id

intervals. From Fig.3, in sub-interval, 0-30°, the current i 1'is zero while i '2and i 3'are negative and positive, respectively. v po = v cb ' ' and v qo = v c '' b '' (16) Therefore, v pq can be mathematically expressed as, v pq = 0.732V L Sin( ω t + 165 ° ) (17)

Similarly, the same computation can be extended to other intervals, respectively which is tabulated in Table I.

TABLE I VOLTAGE ACROSS INTER-PHASE REACTOR ATVARIOUS INTERVALS **Sub-interval *vpq vpq***

0 °− 30 ° 0.732V L Sin( ω t + 165 ° ) 00 0.189VL 300 -0.189VL 30 °− 60 ° 0.732V L Sin( ω t − 45 ° ) 300 -0.189VL 600 0.189VL 60 °− 90 ° 0.732V L cos ( ω t + 15 ° ) 600 0.189VL 900 -0.189VL 90 °− 120 ° 0.732V L Sin( −ω t − 75 ° ) 900 -0.189VL 1200 0.189VL 120 °− 150 ° − 0.732V L cos ( ω t + 135 ° ) 1200 0.189VL 1500 -0.189VL 150 °− 180 ° 0.732V L Sin( −ω t − 15 ° ) 1500 -0.189VL 1500 0.189VL Resultant v pq waveform is shown by Curve-I in Fig.4

Area, under Curve-I for the first quarter cycle is, 15

° ∫ L ω + ° ω = d

(18)

0 As power transformers are normally rated for sinusoidal voltages and currents, area under Curve-I, is therefore equated with area under an approximated sinusoidal waveform shown by Curve-II, overlapped in Fig.4. Area under Curve-II, having RMS,‘ V ’ in the first quarter cycle is,

150

0.732V Sin( t 165 )d t 0.018V

° ∫ 2VCos(6 ω t)d ω t = 0.2357V

(19)

where, ‘ω’ refers to the frequency of AC mains in rad/sec. Equating (18) with (19) yields, V = 0.076V d (20) Peak of the approximated Curve-II, computes to 0.1451 V L, marked in Fig.4. Rating of IPR can be computed as,

I d d VA IPR = d ⌈ │ │ │ │ ⌊ d

d V 2 + V I 2 2 ⌉ │ │ │ │ ⌋

= 0.076V . I 2

= 0.038P (21)

Hence, the combined total rating of D/y/d and IPR amounts to 1.0671 P d, obtained by adding (8) and (21).

III. FORK CONNECTED AUTO- TRANSFORMER SUPPLYING 12-

PULSE, UNCONTROLLED CONVERTER FED RETROFIT VCIMD

*A. Rating Computation for Fork Auto-transformer:*

Fig.5 shows the block schematic for Fork connected auto- transformer supplying 12-Pulse, uncontrolled converter fed Retrofit VCIMD. K 1, K 2and K 3refer to the respective tapings. As secondary windings are not isolated, there may be possibility of inter-converter current paths. To prevent such a situation, IPRs are connected in between respective positive terminals and in between respective negative terminals of the

converters. Winding connections are realised such that both secondary windings getting connected to converters I and II have respective phase voltages15° lagging and leading w.r.t. the main supply. AC supply voltages to transformer primary can be expressed as,

v A = 2V s sin( ω t) (22)

v B = 2V s sin( ω t − 120 ° ) (23)

v C = 2V s sin( ω t + 120 ° ) (24)

where, relates K ‘ 1V *,* sK ’ 2refers and K to 3as,

rms AC supply phase voltage. Fig.6

V A = KV 1 A + KV 2 A and V A 1= KV 1 A − KV 3 B (25)

Solving, K 1= 0.1865 , K 2= 0.1835 and K 3= 0.2988 DC-link voltage, V dcan be expressed using (1) as,

Fig.5. Block Schematic of Fork connected Auto-Transformer supplying

12-Pulse Uncontrolled Converter fed Retrofit VCIMD

V d = (3 6)V s

π (26) Therefore, V zig = K 3 V s = 0.1277V d (27) V long = K 1 V s = 0.3491V d (28) V short = K 2 V s = 0.0784V d (29) Fig.7 shows respective winding currents of Fork connection. Balancing mmf for phase A gives, K 2 (i A 1 + i A 2 + i A ) + K 1 i A + K 3 i C 1 + K 3 i B 2 = 0 (30)

i A

= − K 2 (i A 1 + i A 2 ) + K 3 (i C 1 + i B

2 ) (K 1 + K 2 )

(31)

Similarly, i Band i Ccan be computed by mmf balancing as,

i B

= − K 2 (i B 1 + i B 2 ) + K 3 (i A 1 + i C

2 ) (K 1 + K 2 )

(32)

i C

= − K 2 (i C 1 + i C 2 ) + K 3 (i B 1 + i A

2 ) (K 1 + K 2 )

(33)

From Fig. 7, rms values of currents in zig, long and short windings respectively may be computed as, I zig = (i A 1 ) rms = 0.4082I d (34) I long = (i A ) rms = 0.0609I d (35) I short = (i A 1 + i A 2 + i A ) rms = 0.7836I d (36) Using (27) and (34), VA zig = V zig × I zig = 0.0521P d (37) Similarly, VA long = 0.02126P d and VA short = 0.0618P d From above the rating of Fork auto-transformer, VAFORK is computed as,

= 6 × VA zig + 3 × VA 2

long short

d + 3 × VA = 0.2809P (38)

Fig.6. Block Schematic of Fork connected Auto-Transformer supplying 12-Pulse Uncontrolled Converter fed Retrofit VCIMD

Fig.7 Current Waveforms for Fork Auto-Transformer

Supplying 12-pulse, Uncontrolled Converter Fed Constant Current Load {a}=0.5Id {b}=0.0576Id;{c}=0.1153Id;{d}=0.0341Id;{e}=0.5 576Id;{f}=0.9659Id;{g} = 1.1153Id

*B. Design for Inter-Phase Reactor*

Fig.8. IPR Connected Between Positive Terminals of Converters Fig. 8 shows connections of IPR between positive terminals of the two converters. Diodes D 5and D '5conduct during 0 °− 15 °. Therefore,

v pn = v C 1 ,v qn = v C 2 (39) v C 1 = V s ∠ 135 ° ,v C 2 = V s ∠ 105 ° (40) Resultant voltage across the IPR (v pq ) can be computed as, v pq = 0.7319V s sin( ω t − 150 ° ) (41) Similarly, the same computation can be extended to other intervals respectively. Table II tabulates the resultant data.

TABLE II VOLTAGE ACROSS INTER-PHASE REACTOR AT VARIOUS INTERVALS **Interval *vpq vpq***

0 °− 15 ° 0.7318V S Sin( ω t − 150 ° ) 00 -0.3659VS

150 -0.5174VS 15 °− 45 ° 1.999VSin( S ω t − 30) ° 150 -0.5173VS 450 -0.5173VS 45 °− 75 ° 0.73199V S sin ( ω t + 90) ° 450 750 0.5173VS 0.1894VS 75 °− 105 ° 0.73199VSin( S ω t + 90) ° 750 1050 0.1894VS -0.1894VS 105 °− 135 ° 0.73199V S sin ( ω t + 90) ° 1050 1350 -0.1894VS -0.5175VS

135 °− 165 ° 1.999V S Sin( ω t − 150 ° ) 1350 -0.5173VS 1650 -0.5173VS 165 °− 195 ° 0.73199VSin( S ω t − 30) ° 1650 -0.5173VS 1950 0.1894VS 195 °− 225 ° 0.73199VSin( S ω t − 30) ° 1950 2250 0.1894VS -0.1894VS 225 °− 255 ° 0.73199VSin( S ω t − 30) ° 2250 2550 -0.1894VS -0.5175VS 255 °− 285 ° 1.999VSin( S ω t + 90) ° 2550 -0.5175VS 2850 0.5175VS 285 °− 315 ° 0.73199V S Sin( ω t − 150 ° ) 2850 0.5175VS 3150 0.1894VS

315 °− 345 ° 0.73199V S Sin( ω t − 150 ° ) 3150 0.1894VS 3450 -0.1894VS

345 °− 360 ° 0.73199VSin( S ω t − 150) ° 3450 -0.1894VS 3600 -0.3659VS Resultant v pq therefore, is obtained as shown in Fig.9

Area under Curve-I for the positive half cycle is computed as,

90 °= ∫ v pq dwt = 0.12077V d

(42)

30

° As transformers are normally rated for sinusoidal voltages and currents, area under curve-I, v pq is compared to that of

Curve-II with rms ‘V’. Area under Curve-II in the positive half cycle is computed as,

90°= ∫ 2VSin(3( ω t − 30 ° ))dwt = 0.942V

(43)

30

°

Equating equations (42) and (43),

V = 0.128V d (44) Peak of approximated sinusoid signal computes to 0.4236Vs as per marked in Fig.9. Rating of IPR is,

I d d

VA IPR = d d

d ⌈ │ │ │ │ ⌊ V 2 + V I 2 2 ⌉ │ │ │ │ ⌋

0.128V I 2 0.06405P = = (45)

Gross IPR rating amounts to, VA IPR(TWO) = 0.1281P d (46)

Henceforth, the combined rating of Fork connected auto- transformer and two IPRs amount to 0.4089 P d, as obtained by adding (38) and (46).

IV. RESULTS AND DISCUSSION To improve the quality of current drawn from AC mains, a comparative investigation has been carried out between D/y/d and Fork topologies with main objective being to investigate which topology gives rise to lower magnetic rating. Respective topologies have been designed and simulated in MATLAB environment to manifest their power quality performance for retrofit VCIMD.

Fig.10 shows the dynamic response for D/y/d connected, 12-Pulse, Uncontrolled Converter fed retrofit VCIMD for starting and load perturbation modes respectively. The plot consists of reference and actual speed, reference motor currents, actual motor currents, motor developed torque and load torque, utility supply, supply line current and DC-link voltage respectively. Fig.12 portrays two cycles of supply current on FL along with spectrum showing 6.12% THD. The comparison between various power quality parameters on FL and LL is tabulated in Table III.

Fork connected auto-transformer fed VCIMD is simulated in MATLAB environment. Fig.11 shows the dynamic response of the retrofit drive for starting and load perturbation

Fig.9. Voltage across IPR for Fork transformer supplying 12-Pulse

Uncontrolled Converter fed Non-Linear Load Curve I: Actual Voltage, Curve-II: Approximated Sinusoidal Voltage

respectively. The plot consists of reference and actual speeds, reference motor currents, actual motor currents, motor developed torque and load torque, utility supply, supply line

**400 200 0 -200-400 1000**

**-100600**

**400**

**200**

**0**

**)D(**current and DC-link voltage respectively. Fig.13 shows two cycles of supply current waveform with necessary harmonic

**200**

**0**

**-200200 )E(0**

**-200200 ) F(0**

**-200600 ) G(400 200 0 -2000.2 0.3 0.4 0.5 Time(sec) 0.6 0.7 0.8 0.9 1** Fig.10.Dynamic Response of D/y/d, 12-pulse , Uncontrolled Converter fed retrofit VCIMD for (A) Source Voltage, (B) Source Current, (C) DC-Link Voltage, (D) Rotor Speed, (E) Reference Currents, (F) Actual Currents and (G) Developed Torque and Load Torque

**400 200 0 -200-400 1000**

**-100600**

**400**

**200**

**0**

**)D(200 0**

**-200200 )E(0**

**-200200 ) F(0**

**-200600 ) G(**Fig.11 Dynamic Response of Fork, 12-pulse, Uncontrolled Converter fed retrofit VCIMD for (A) Source Voltage, (B) Source Current, (C) DC-Link Voltage, (D) Rotor Speed, (E) Reference Currents, (F) Actual Currents and (G) Developed Torque and Load Torque **400 200 0 -2000.2 0.3 0.4 0.5 Time(sec)**

**0.6 0.7 0.8 0.9 1**

spectrum when drive is on FL. In this case, the THD in the line current drawn from the supply mains is observed 5.84% .Necessary parameters relating to supply current power quality have been tabulated in Table III and Table IV provides the comparison between magnetic ratings.

TABLE III COMPARISON OF POWER QUALITY INDICIES OF A RETROFIT DRIVE VCIMD FED FROM 12-PULSE UNCONTROLLED CONVERTER

Topo-

THD(%) Distortion

Power logy

Factor

Factor

LL FL LL FL LL FL LL FL

D/y/d 8.30 6.12 0.99 0.99 0.98 0.97 0.97 0.97

Fork 8.14 5.84 0.99 0.99 0.98 0.97 0.97 0.96

TABLE IV RATING OF MAGNETICS IN DIFFERENT CONVERTER TOPOLOGIES Rating expressed as Percentage

D/y/d Fork Total DC-Link Load (Pd) Power Transformer 102.91% 28.09% IPR 3.80% 12.81%

Total Magnetic Rating 106.71% 40.89%

Fig.12. (A) Supply current (B) THD analysis of supply current for D/y/d connected transformer, supplying 12-pulse uncontrolled converter fed retrofit drive VCIMD

Fig.13. (A) Supply current (B) THD analysis of supply current for Fork connected transformer, supplying 12-pulse uncontrolled converter fed retrofit drive VCIMD

V. CONCLUSION A comparative investigation between D/y/d and Fork connected transformer topologies supplying 12-Pulse, Uncontrolled Converter fed retrofit VCIMD has been carried

Displacement factor

out with an objective to prove that Fork connection amounts to lesser rating and saving in magnetics.

Based on design and MATLAB simulations, it has been observed that the total rating for transformer and IPR amounts to 106.71% in D/y/d and 40.89% in Fork respectively of the total DC-link load for same rating retrofit VCIMD. The comparison shows similar performance level both from drive dynamics and supply power quality aspects respectively. Therefore, use of Fork topology saves copper and leads to reduction in cost and improvement in power quality.

VII.APPENDIX

Induction motor specifications: 30 HP, 3-phase, 4 pole, Y- Connected, 415V, 45A, 50Hz, Rs=0.251 Ω, Rr= 0.249 Ω, Xls= Xlr= 0.439 Ω, Xm=13.085 Ω, J= 0.305Kgm2. PI Controller parameters: KP= 350, Ki=50. DC link filter parameters: Ld= 2mH, Cd=1500μF

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